

Multiplying and Dividing Inequalities by Negative Numbers

Name: KEY PER Class: _____

Let's think about what makes sense:

True or False?

$$(1) 1 < 5 (-1)$$

Now, multiply each side by -1.

True or False?

$$-1 < -5$$

If this is false, what would we have to change to make it true?

$$-1 \underline{>} -5$$

True or False?

$$(-2) - 3 > -8 (-2)$$

Now, multiply each side by -2.

True or False?

$$6 > 16$$

If this is false, what would we have to change to make it true?

$$6 \underline{\leq} 16$$

True or False?

$$10 < 25$$

Now, divide each side by -5.

$$\frac{-10}{-5} < \frac{25}{-5}$$

True or False?

$$-2 < -5$$

If this is false, what would we have to change to make it true?

$$-2 \underline{\geq} -5$$

What do you notice? What happens each time we multiply or divide by a negative number?

The inequality is false and we need to change the inequality direction

Solving and graphing by multiplying or dividing with negatives:

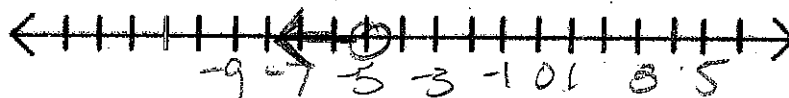
Examples:

1. $-5n > 25$

$$\begin{array}{r} \overline{-5} \quad \overline{-5} \\ n < -5 \end{array}$$

Check:

$$\begin{array}{l} n = -10 \\ -5(-10) > 25 \\ 50 > 25 \end{array}$$

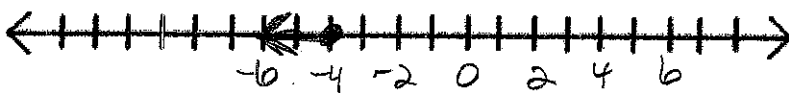


2. $64 \leq -16m$

$$\begin{array}{r} \overline{-16} \quad \overline{-16} \\ -4 \geq m \end{array}$$

Check:

$$\begin{array}{l} m = -10 \\ 64 \leq -16(-10) \\ 64 \leq 160 \end{array}$$

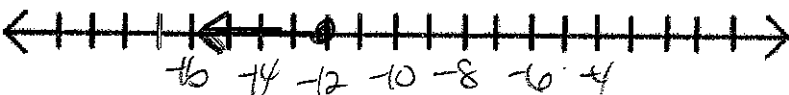


3. $-\frac{3}{4}x \geq 9$

$$\begin{array}{r} \overline{-\frac{3}{4}} \quad \overline{-\frac{3}{4}} \\ x \leq -12 \end{array}$$

Check:

$$\begin{array}{l} \text{let } x = -16 \\ -\frac{3}{4}(-16) \geq 9 \\ 12 \geq 9 \end{array}$$

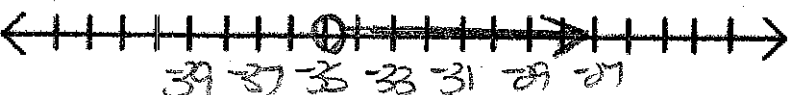


4. $7 - \frac{k}{7} < 5 - 7$

$$\begin{array}{r} \overline{-\frac{1}{7}} \quad \overline{-\frac{1}{7}} \\ k > 35 \end{array}$$

Check:

$$\begin{array}{l} \text{let } k = 28 \\ 7 - \frac{28}{7} < 5 - 7 \\ 4 < 5 \end{array}$$



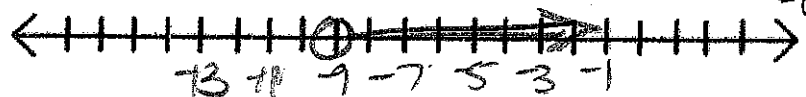
Try these:

5. $-6n < 54$

$$\begin{array}{r} \overline{-6} \quad \overline{-6} \\ n > -9 \end{array}$$

Check:

$$\begin{array}{l} n = 0 \\ -6(0) < 54 \\ 0 < 54 \end{array}$$

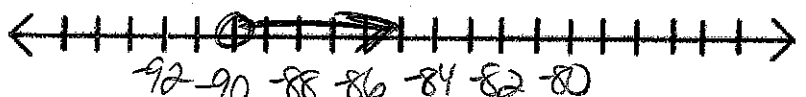


6. $81 > -0.9y$

$$\begin{array}{r} \overline{-0.9} \quad \overline{-0.9} \\ -90 < y \end{array}$$

Check:

$$\begin{array}{l} y = 0 \\ 81 > -9(0) \\ 81 > 0 \end{array}$$

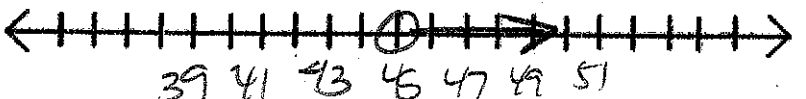


7. $3 - \frac{p}{3} < -15 - 3$

$$\begin{array}{r} \overline{-\frac{1}{3}} \quad \overline{-\frac{1}{3}} \\ p > 45 \end{array}$$

Check:

$$\begin{array}{l} \text{let } p = 60 \\ \frac{-60}{3} < -15 \\ -20 < -15 \end{array}$$



8. $\frac{h}{6} - \frac{h}{4} > -7 - 4$

$$h < 28$$

Check:

$$\begin{array}{l} h = 0 \\ -\frac{0}{4} > -11 \\ 0 > -11 \end{array}$$

